

Long-range mutual synchronization of spin Hall nano-oscillators

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The spin Hall effect in a non-magnetic metal with spin-orbit coupling injects transverse spin currents into adjacent magnetic layers, where the resulting spin transfer torque can drive spin wave auto-oscillations. Such spin Hall nano-oscillators (SHNOs) hold great promise as extremely compact and broadband microwave signal generators and magnonic spin wave injectors. Here we show that SHNOs can also be mutually synchronized with unprecedented efficiency. We demonstrate mutual synchronization of up to nine individual SHNOs, each separated by 300 nm. Through further tailoring of the connection regions we can extend the synchronization range to 4 μm . The mutual synchronization is observed electrically as an increase in the power and coherence of the microwave signal, and confirmed optically using micro-Brillouin light scattering microscopy as two spin wave regions sharing the same spectral content, in agreement with our micromagnetic simulations.

Spin transfer torque (STT)^{1–3} from a spin-polarized current can inject high-amplitude spin waves^{4,5} in magnonic circuits based on so-called nano-contact spin torque oscillators (STNOs)^{6–13}. As the wavelength of the injected spin waves is proportional to the size of the nano-contact¹⁴, truly nanoscopic, dipolar-exchange-dominated¹⁵ spin waves with a highly directional^{16–18} nature can be generated. With the recent advent of the spin Hall effect (SHE)^{19–21} substantial STT can also be exerted on a single ferromagnetic layer via a pure transverse spin current generated by a lateral current in an adjacent non-magnetic layer with spin-orbit coupling. The corresponding microwave signal generators, so-called spin Hall nano-oscillators (SHNOs)^{22–27}, exhibit a number of advantages compared to STNOs, such as easier nano-fabrication, reduced current through the magnetic layers, and direct optical access to the magnetodynamically active area.

The high nonlinearity²⁸ of STNOs can promote spin-wave-mediated mutual^{29–32} and driven³³ synchronization of multiple nano-contacts^{29,30,32,33}. Whereas SHNOs show a similar nonlinearity, are readily injection-locked to external microwave currents³⁴, and have been numerically predicted to exhibit mutual synchronization³⁵, any experimental demonstration is still lacking. A particular limitation of the SHNOs studied to date is the self-localized nature of the dominant mode, which cuts off spin-wave-mediated interactions. Although nanoconstriction SHNOs show signs of a second, more extended mode²⁵, they have primarily been studied with their magnetization in the plane, where it is known from STNOs that even the inherently propagating mode suffers localization from the magnetic field landscape^{16,17}. To reduce this localization³⁶, we here study multiple nanoconstriction SHNOs in out-of-plane fields. We observe strong and robust mutual synchronization of as many as nine independent nanoconstrictions, each separated from its neighbour by 300 nm. Similarly, in double-constrictions with the same geometry, we demonstrate mutual synchronization for separations up to 1.2 μm . Finally, by reducing the width of the regions connecting the two nanoconstrictions we can use the negative damping from the sub-critical current density to extend the synchronization up to separations as large as 4 μm .

Figure 1 summarizes the basic structural and electrical properties of our SHNOs (see Methods). Figure 1a schematically presents the material stack, the device layout, and the applied field vector, Fig. 1b shows a scanning electron microscope (SEM) picture of a SHNO with nine nanoconstrictions ($w = 120$ nm wide and separated by $d_{cc} = 300$ nm), and Fig. 1c shows a spatial map of the lateral charge current density in the Pt layer, to which the transverse spin current entering the NiFe layer is proportional. As shown in Fig. 1d, the device resistance increases linearly with the number of constrictions; each 120 nm constriction adds 39 Ω , while the additional series resistance is 70 Ω . The in-plane angular dependence of the magnetoresistance (MR versus φ) can be fitted well (inset of Fig. 1d) by an expression based on anisotropic magnetoresistance (AMR) with a weak in-plane anisotropy of about 80–130 Oe along the length of the nanoconstrictions.

The polar field angle $\theta = 80^\circ$ was chosen to achieve positive nonlinearity in the nanoconstriction region, which is expected to reduce the localization of the auto-oscillations^{28,37,38}. The in-plane angle was $\varphi = 22^\circ$ – 26° (except in Fig. 6) to realize sufficient electrical sensitivity to angular deflections (that is, auto-oscillations) of the magnetization.

Figure 2a shows the current dependence of the microwave electrical signal generated by a single nanoconstriction in a magnetic field of 0.72 T, tilted $\theta = 80^\circ$ out-of-plane, with its in-plane component being tilted 66° away from the current direction ($\varphi = 24^\circ$). At low currents, the signal is weak and exhibits the same redshifting current dependence as for in-plane fields²⁵. At intermediate currents, the frequency shows a clear minimum above which the frequency blueshifts, the microwave power increases (Fig. 2a(II,III)), and the linewidth shows a non-monotonic behaviour (Fig. 2a(IV)). Measurements on a further seven similar single nanoconstrictions are shown in Supplementary Methods Section A.

The more interesting case of double nanoconstrictions is presented in Fig. 2b–f, which summarizes our results for five different nanoconstriction separations, ranging from 300 nm to 1.2 μm (an additional set of measurements of double

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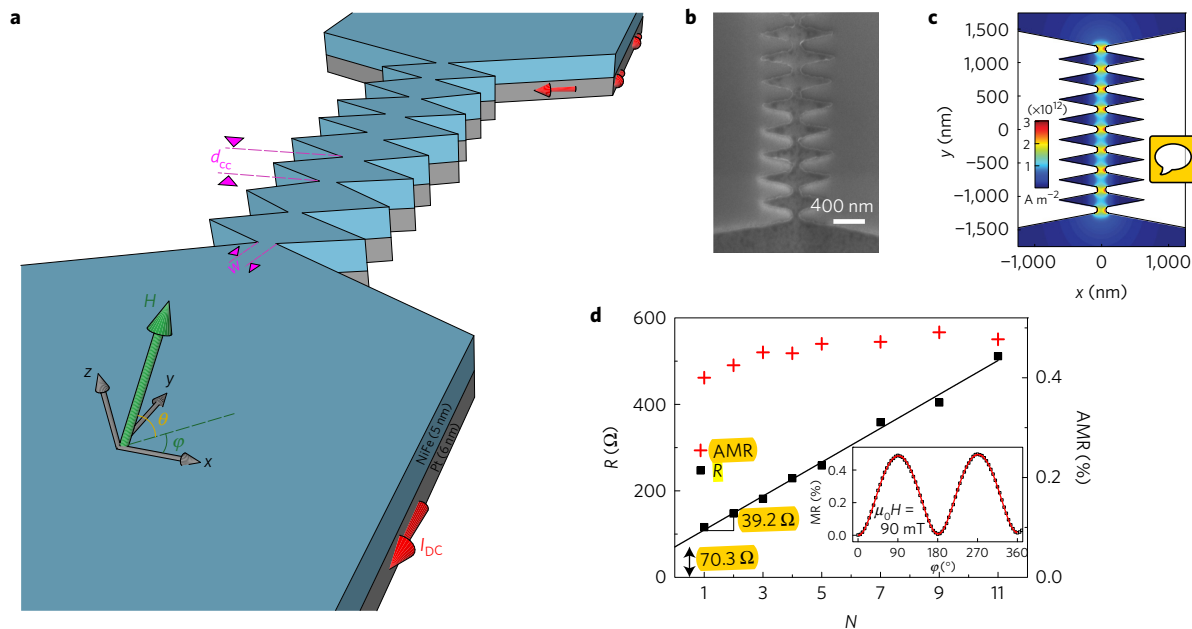


Figure 1 | Device schematic, current distribution, and static measurements. **a**, A schematic illustration of the general SHNO layout, showing the patterned Py/Pt bilayer and the field and current directions used throughout the article. **b**, A scanning electron microscope (SEM) image of a SHNO with nine 120-nm-wide nanoconstrictions each separated by $d_{cc} = 300$ nm. **c**, Calculated lateral current density in the Pt layer for a total current of $I_{d.c.} = 2$ mA. **d**, Measured SHNO resistance (R) and anisotropic magnetoresistance (AMR) versus number of nanoconstrictions (N). Each nanoconstriction adds about 39Ω . Inset: angular field scan of the resistance of a SHNO with nine nanoconstrictions showing an AMR of 0.5%. The red line is a fit allowing for a small in-plane uniaxial anisotropy field (12.9 mT) along the nanoconstrictions.

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1 nanoconstrictions is shown in Supplementary Methods Section B).
 2 At low current, each device shows two individual and decoupled
 3 signals, with qualitatively the same behaviour as in Fig. 2a(I).
 4 The two signals can cross in frequency, as in Fig. 2c, without
 5 interference, frequency pulling or phase locking, consistent with
 6 two non-interacting auto-oscillating regions. The situation changes
 7 dramatically at higher currents, where the frequencies blueshift.
 8 For the two closest nanoconstrictions (Fig. 2b(I)), the two weak
 9 signals merge into a much stronger single signal at about 2.4 mA,
 10 indicating their mutual synchronization. This synchronized
 11 state remains stable at all higher investigated currents. At a
 12 separation of 500 nm, a current of about 3.2 mA is required for
 13 mutual synchronization; again, the synchronized state remains
 14 stable at all higher currents. At a separation of 700 nm, mutual
 15 synchronization first appears at 2.7 mA, is then broken up, until
 16 the nanoconstrictions again synchronize at about 3.3 mA. Finally,
 17 the nanoconstrictions separated by 900 nm and $1.2 \mu\text{m}$ also show
 18 clear regions of mutual synchronization, albeit for a more limited
 19 current range. At separations greater than $1.2 \mu\text{m}$ we were not able
 20 to observe synchronization in this geometry.

21 As expected, the mutually synchronized state is characterized
 22 by both a higher microwave power as compared to the sum of
 23 the individual SHNOs, as well as a reduced linewidth compared
 24 to the unsynchronized SHNOs²⁸. In most cases, this improvement
 25 is only gradual (Fig. 2b,c and Supplementary Methods), whereas
 26 in others the mutual synchronization leads to a more abrupt
 27 improvement (Fig. 2d). Both scenarios are consistent with what
 28 is expected from theory and experiments in the literature on
 29 mutual synchronization of STNOs. The gradual case is predicted
 30 theoretically as a consequence of the weak coupling and varying
 31 difference in the free-running frequencies of two oscillators²⁸. At
 32 the onset of synchronization, the relative phase is the largest with
 33 one of the oscillators trailing the other in phase.

34 If the free-running frequency of the slower oscillator has a
 35 stronger current dependence than the other, the relative phase will
 36 decrease with current, reach zero when the free-running frequencies

coincide, then change sign, and eventually again reach a maximum
 negative value at the other synchronization boundary. Both the
 power and the linewidth of the mutually synchronized state are
 direct functions of the relative phase such that the power (linewidth)
 shows a maximum (minimum) when the relative phase crosses zero.
 In the case of non-crossing intrinsic frequencies, the relative phase
 will never reach zero, but still varies with the intrinsic frequency
 difference, with an optimum power and linewidth when the relative
 phase has a minimum.

One may notice a substantial increase in power fluctuations
 in the mutually synchronized state (for example, column III in
 Fig. 2), which to a lesser extent also seems present in the single
 nanoconstriction (Fig. 2a). This might be related to slow frequency
 jitter, $1/f$ noise, or otherwise coloured noise, on timescales similar
 to the data acquisition of the spectrum analyser, and with frequency
 deviations greater than the intrinsic linewidth^{39–42}. We note that
 the appearance of large power fluctuations correlates with a narrow
 linewidth, which corroborates this picture. When we average
 four scans (Supplementary Figs 2–4) the power fluctuations are
 greatly reduced.

To learn more about the observed mutual synchronization,
 we have carried out micromagnetic simulations of double
 nanoconstrictions in a tilted magnetic field (Fig. 3). The two
 simulated nanoconstrictions differed in width by 8 nm, to mimic
 the natural variation of the fabrication process. We first simulated
 each nanoconstriction separately (Fig. 3a). The narrower SHNO
 shows an earlier onset of the auto-oscillations as a function
 of current, consistent with the higher current density. More
 importantly, the experimentally observed overall trend of the
 frequency first redshifting, then showing a minimum, and finally
 blueshifting with increasing current, is well reproduced by the
 simulations. To better understand what governs this behaviour we
 show the spatial profiles of the auto-oscillations in the insets of
 Fig. 3a. We find that the auto-oscillations emerge from the edges
 of the nanoconstrictions, similar to what has been reported for
 nanoconstriction and nanowire SHNOs^{24,25,35,43} in in-plane fields.

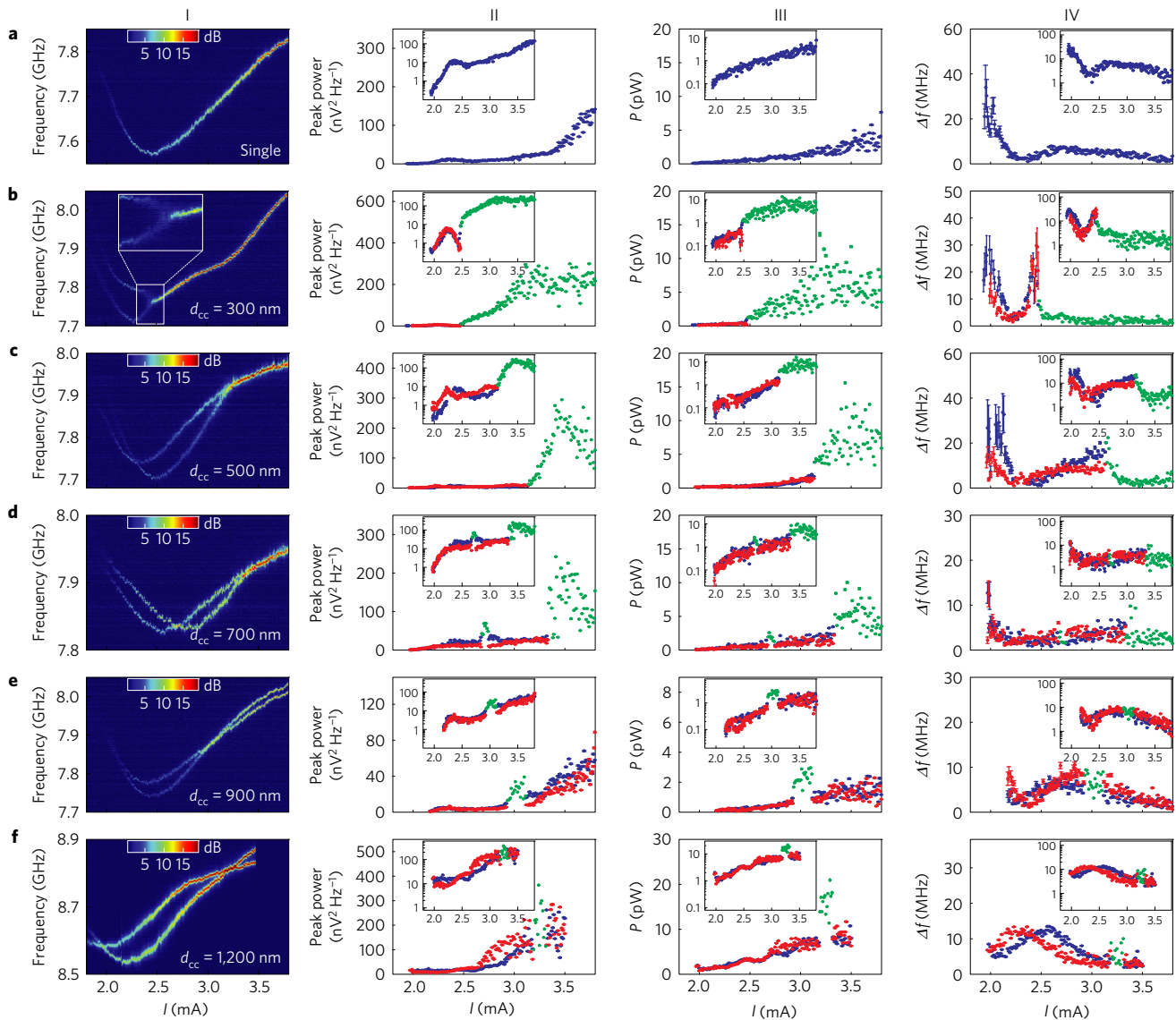


Figure 2 | Electrical microwave characterization. Results of a single nanoconstriction (a), and double nanoconstrictions with $W=120$ nm and separated by $d_{cc}=300$ nm (b), $d_{cc}=500$ nm (c), $d_{cc}=700$ nm (d), $d_{cc}=900$ nm (e) and $d_{cc}=1,200$ nm (f), in an applied field of 720 mT along $\varphi=24^\circ$ and $\theta=80^\circ$. The inset in b shows a zoom of the synchronization region. Column I gives the power spectral density versus current of the SHNO devices. Column II gives the microwave peak power density versus current of the signal in column I. Column III gives the total microwave power versus current of the signal. Column IV gives the Lorentzian linewidth versus current. Columns II and III show a sharp increase of the peak power and the total microwave power, respectively, as the two nanoconstrictions synchronize. A substantial improvement of the linewidth upon synchronization is shown in column IV.

1 However, in our case of out-of-plane fields, the auto-oscillation
 2 region expands into the nanoconstriction with increasing current,
 3 and the point of maximum intensity moves inwards. Consequently,
 4 the mode experiences a strongly varying field landscape such
 5 that the net effect is a frequency redshift as the mode leaves
 6 the edges, followed by a blueshift as it further expands into the
 7 bridges connecting the nanoconstrictions. The response of the
 8 simultaneously excited pair of nanoconstrictions is shown in Fig. 3b.
 9 At low current, the auto-oscillations are virtually indistinguishable
 10 from the individual simulations, suggesting a vanishing interaction
 11 between the auto-oscillating regions in this regime. However,
 12 as these regions expand at intermediate current, their mutual
 13 interaction can be observed both as substantial inter-modulation
 14 and as a gradual reduction of their frequency difference. Further
 15 mode expansion at higher current leads to stronger interaction,
 16 which finally makes the two modes synchronize at about 2.5 mA.

17 In the mutually synchronized state, only a single constant
 18 amplitude signal is generated (Fig. 3c), and the relative phase

19 between the two nanoconstrictions remains constant over time
 20 (Fig. 3d). In contrast, the unsynchronized state is characterized
 21 by an amplitude that exhibits a steady beating (Fig. 3c), and a
 22 continuously varying relative phase (Fig. 3d). Figure 3e shows
 23 fast Fourier transforms (FFTs) and spatial maps of the two states,
 24 with mutual synchronization characterized by a single peak and
 25 both nanoconstrictions sharing the same spectral content, and the
 26 unsynchronized state showing two distinct peaks, each generated
 27 by one of the two nanoconstrictions. The rightmost inset in Fig. 3e
 28 shows a map of the instantaneous phase of all precessing spins in the
 29 synchronized state. One can clearly see two separate regions, each
 30 having its own phase, and an S-shaped boundary between those two
 31 regions where the phase changes continuously from the value of one
 32 region to the other. The phase map indicates that the interaction
 33 between the auto-oscillating regions takes place at this boundary
 34 and is mediated by direct exchange.

35 We can also confirm both the electrical and the simulated results
 36 using scanning micro-focused Brillouin light scattering microscopy

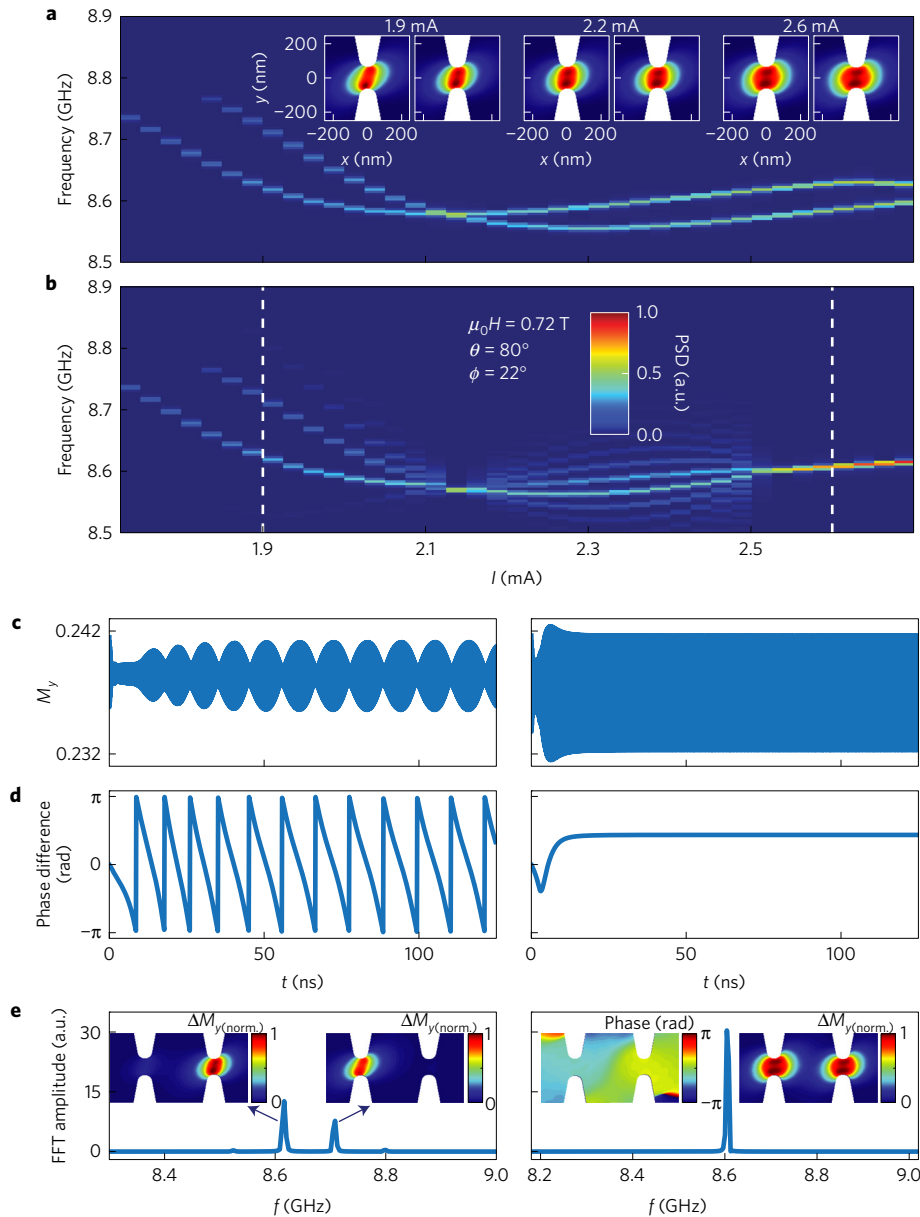


Figure 3 | Micromagnetic simulations. **a,b**, Power spectral density versus current of the double free-running (**a**) and interacting (**b**) nanoconstriction SHNOs with the widths, W_1 of 117 nm and 125 nm and a separation of $d_{cc} = 500$ nm in an applied field of 720 mT along the $\varphi = 22^\circ$ and $\theta = 80^\circ$ direction. The insets organized pairwise in **a** show the spatial distribution of the power spectral density of the auto-oscillations at the selected currents demonstrating the expansion of the corresponding modes as the applied current increases. The left and right panels in the pairs correspond to the larger and smaller nanoconstrictions, respectively. **c**, Averaged magnetization oscillation in time domain taken at 1.9 mA (left panel) and 2.6 mA (right panel). **d**, Phase difference between the two nanoconstriction. **e**, Power spectral density of the M_y component of the magnetization taken at 1.9 mA and 2.6 mA respectively. The colour plots in the insets present the spatial distribution of the spin wave amplitudes in the unsynchronized state (left) and the spin wave amplitude and phase in the synchronized state (right).

1 (μ -BLS)^{4,5}. Figure 4 shows two rows of spin wave maps on the
 2 same device as in Fig. 2d. The upper row corresponds to an
 3 unsynchronized state, whereas the bottom row shows similar maps
 4 in the mutually synchronized state. Since the spectral resolution
 5 of μ -BLS is insufficient to resolve the actual linewidth of the
 6 microwave signals and their separation in the unsynchronized
 7 state (Fig. 4b), we do not expect maps of the two states to look
 8 very different from each other. This is confirmed in column III
 9 in Fig. 4a, where maps for the two states show little qualitative
 10 difference. However, as all counts are binned into separate spin
 11 wave frequencies we can focus on the high and low ends of the μ -BLS
 12 peak, and plot spatial maps of the frequency-selected μ -BLS counts;
 13 maps at lower spin wave frequencies are shown in columns I & II,

and maps at higher spin wave frequencies in columns IV & V. 14
 We then clearly see that whereas the maps of the mutually synchronized 15
 state do not change other than in their overall intensity, the maps 16
 of the unsynchronized state change entirely, indicating how the spin 17
 waves in the two nanoconstrictions have different frequencies. At 18
 the lowest mapped frequency there are essentially no counts in the 19
 lower nanoconstriction, and at the highest mapped frequency there 20
 are very few counts in the upper nanoconstriction. This is further 21
 quantified in Fig. 4e, where we plot the fraction of counts in the 22
 upper and lower halves of the maps for both the synchronized and 23
 non-synchronized case. Clearly, the relative counts do not change 24
 in the synchronized state, implying that their spectral spin wave 25
 content in both nanoconstrictions is identical. Interestingly, in the 26

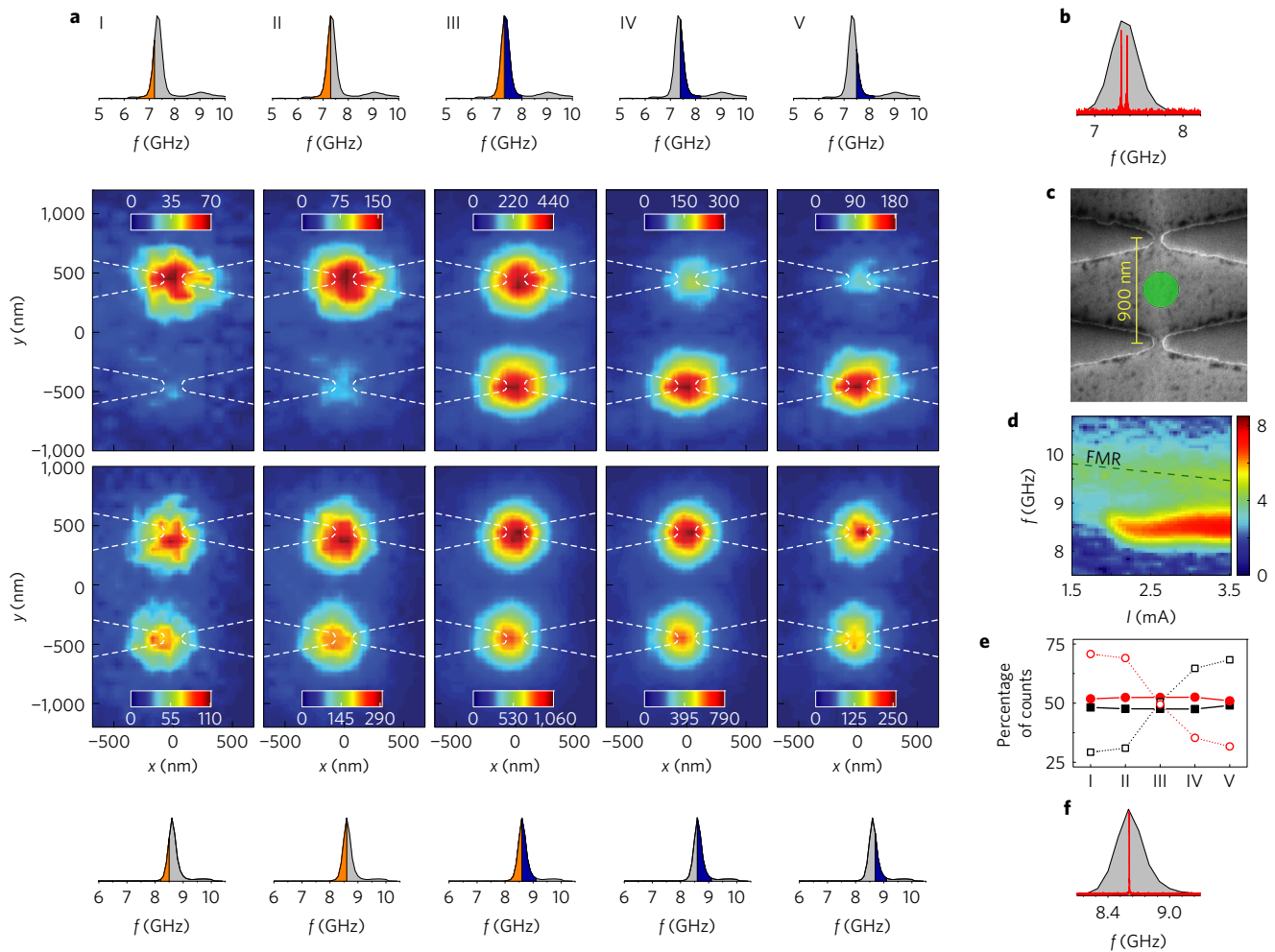


Figure 4 | μ -BLS measurements. **a**, Columns I–V show spatial maps of the μ -BLS counts in the unsynchronized (upper maps) and synchronized (lower maps) state, with a frequency selection indicated by the coloured regions in the spectra above and below each panel. **b**, The electrically measured microwave signal (red) overlaid on top of the total μ -BLS spectrum in the unsynchronized state, taken at a current of $I_{d.c.} = 2.6$ mA and in a field of 553 mT along $\theta = 80^\circ$ and $\varphi = 3^\circ$. **c**, SEM picture of the SHNO. **d**, Spectra of the μ -BLS (logarithmic scale) as a function of the applied current as measured at the centre of the sample $x = y = 0$ (green spot in **c**), in a field of 640 mT, again along $\theta = 80^\circ$ and $\varphi = 3^\circ$ the FMR frequencies have a small negative slope due to the Oersted field (reinforced with the green dashed line as a guide to the eye). **e**, Fraction of the counts in the upper (circles) and lower (squares) half of the synchronized (filled symbols) and unsynchronized (open symbols) state, respectively. **f**, The electrically measured microwave signal (red) and total μ -BLS spectrum in the synchronized state, taken at a current of $I_{d.c.} = 3.5$ mA and the same conditions as in **d**.

space between the constrictions, $x = y = 0$ as shown in Fig. 4c, a measurable intensity of spin waves is detected (Fig. 4d). We note that these excitations exhibit frequencies below the local ferromagnetic resonance (FMR; the FMR frequencies have a small negative slope due to the Oersted field created by the current running through the Pt layer) and are significantly more intense, consistent with auto-oscillations. The direct observation of finite excitations between the nanoconstrictions corroborates our micromagnetic simulations and suggests that direct exchange promotes the observed mutual synchronization. The observed upper limit of $1.2 \mu\text{m}$ for the mutual synchronization of two SHNOs is probably a consequence of damping in the bridge connecting the two nanoconstrictions. If so, it should be possible to further extend the maximum range of mutual synchronization by reducing the damping in the bridge. This can in principle be achieved through the same spin Hall effect driving the auto-oscillations in the nanoconstrictions^{44–46}. By reducing the width of the bridge, and hence the current spread, we should be able to hold the local current density just below the auto-oscillation threshold and greatly enlarge the distance that the auto-oscillating regions can drive sub-threshold precession between the nanoconstrictions. Figure 5a shows the electrical

microwave signal of such a double-SHNO device where two 140 nm nanoconstrictions, separated by $4 \mu\text{m}$, are connected by a bridge that only opens up about 5° , Fig. 5c. When a current less than 2.6 mA is driven through the device, two individual microwave signals appear. When the current is further increased, the two signals merge, the power increases, and the linewidth improves (see Supplementary Section B and Supplementary Fig. 3), all strong indications that the two SHNOs have indeed synchronized over a distance as great as $4 \mu\text{m}$. We expect that as the current is increased the auto-oscillating regions would expand towards the centre of the connecting bridge as the points where the local current density reaches the auto-oscillation threshold move inwards. Figure 5b plots μ -BLS line scans along the nanoconstrictions centre, x direction of the device, and clearly demonstrates that the auto-oscillating regions actually expand inwards, whereas their outer boundaries remain static. The approximately linear current dependence of the expansion also reflects the linear profile of the width of the bridge. Figure 5c shows a spatial μ -BLS map of the device in the same field and at a current of 2.4 mA. It is clear from the map that the auto-oscillation regions reside close to the nanoconstrictions, but inside the connecting bridge. In a device with $4 \mu\text{m}$ nanoconstriction

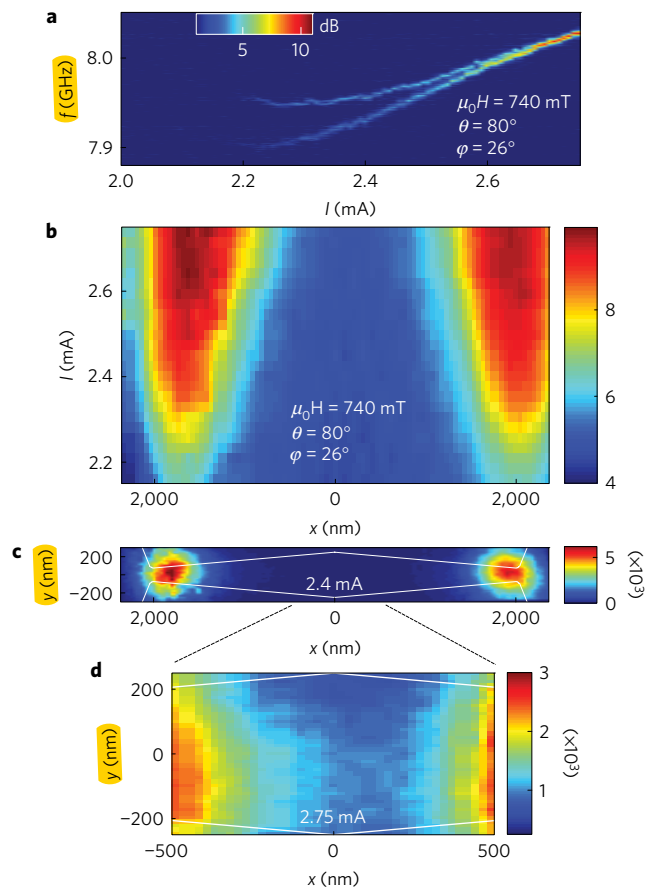


Figure 5 | Long-range synchronization. **a**, Power spectral density versus current of two 140 nm nanoconstrictions separated by 4 μm in an applied field of 740 mT along $\varphi = 26^\circ$ and $\theta = 82^\circ$. **b**, μ -BLS line scans (logarithmic scale) through the centre of the device at increasing currents. **c**, μ -BLS spatial map of the same device in the same field and at an applied current of 2.4 mA. **d**, μ -BLS scans through the central part of the device at 2.75 mA.

separation, the actual separation of the centres of the two oscillating regions is hence slightly reduced to about 3.7 μm . For a drive current of 2.75 mA—that is, in the synchronized state—we clearly find a non-zero amplitude of precession in the middle of the bridge on the same frequency as the two auto-oscillation regions (Fig. 5d). The long-range nature of the mutual synchronization hence appears to be a combined effect of both reduced damping and the two auto-oscillation regions approaching each other at high current.

Having demonstrated the ability to synchronize two oscillators over large distances, we now focus on how many more oscillators we can mutually synchronize. We fabricated SHNOs with multiple nanoconstrictions ranging from two to eleven with a fixed centre-to-centre separation of 300 nm. The largest number of mutually synchronized nanoconstriction we have observed is nine (Fig. 6); other examples of three and nine nanoconstrictions are shown in the Supplementary Methods. Although the overall synchronization behaviour is similar to that of double nanoconstrictions, we now also observe partially synchronized states. As shown in Fig. 6a, for low drive currents, each individual nanoconstriction generates its own separate microwave signal whose frequency first decreases with current. As each nanoconstriction passes its minimum frequency, their mutual interactions increase, promoting first a partially synchronized state, probably among neighbouring oscillators, which eventually leads to a globally synchronized state at about 3.29 mA. The maximum power in this regime reaches 54 pW—that is, significantly higher than the sum of the output

powers of the free-running oscillators, but still less than the theoretical maximum increase of $N^2 = 81$, which indicates a finite relative phase difference between the individual oscillators. We also find that the nine mutually synchronized nanoconstrictions exhibit the lowest linewidth of about 2 MHz. For an accurate comparison between different numbers of nanoconstrictions we use the results from the averaged scans in the Supplementary Methods to mitigate the large scatter⁴⁰ observed in Fig. 2. Comparing linewidths at 3 mA we find about 10 MHz for single nanoconstrictions (Supplementary Fig. 1), 5 MHz for double nanoconstrictions (Supplementary Fig. 2), and 3–4 MHz for a triple nanoconstriction (Supplementary Fig. 4). This approximately inverse dependence on the number of nanoconstrictions is consistent with a total mode volume that grows linearly with the number of mutually synchronized nanoconstrictions mitigating the effect of the thermal fluctuations^{47,48}.

It is interesting to note that if we reduce the applied field substantially from 745 mT to 576 mT (Fig. 6g), while keeping the field direction about the same, we can no longer realize a mutually synchronized state. Instead, we mainly see individual signals, which redshift over a much larger current range. As the weaker field leads to a smaller out-of-plane angle of the magnetization, this corroborates our earlier conclusion that a certain minimum out-of-plane magnetization angle is required to drive the mode expansion, make the mode leave the nanoconstriction edge, and finally promote strong interaction between neighbouring oscillators. In other words, the applied field controls both the dispersion of the frequencies and the interaction between the oscillators.

To further verify the mutual synchronization of all nine nanoconstrictions, μ -BLS is utilized to spatially map both a synchronized (Fig. 6d–f), and an unsynchronized (Fig. 6g–i) state, of the same device as shown in Fig. 6a–c. In the synchronized state, the μ -BLS maps confirms that all nine nanoconstrictions have both the same frequency and similar amplitudes (Fig. 6e,f). Since our diffraction limited resolution (360 nm) cannot resolve the individual oscillators with 300 nm centre-to-centre spacing, the nine oscillators appear as a continuous auto-oscillating region. However, micromagnetic simulations still confirm that the synchronized state consists of nine individual auto-oscillating regions interacting via their evanescent tails. In contrast, the μ -BLS map of the unsynchronized, or possibly partially synchronized state, shows a varying frequency along the connected nanoconstrictions, with some possible clustering of neighbouring oscillators, which might indicate partial or pairwise synchronization.

It is noteworthy that the total power is on par with typical GMR-based devices, despite the much lower AMR, which indicates that the coherent SW power in the synchronized SHNOs is very high. Although the microwave power is still orders of magnitude lower than that of magnetic tunnel junction (MTJ)-based STNOs, which can surpass 2 μW (ref. 49), we expect three terminal SHNO devices to perform even better. In such devices, mutually synchronized SHNOs would generate the SW power, and MTJs, fabricated on top of each oscillating region, would convert these SWs into microwave power. As the drive current path and the MTJ current paths can then be optimized individually, MTJs with much higher tunnelling magnetoresistance could be used instead of today's low-resistance-area MTJ-based STNOs, providing yet another increase in power.

Although mutual synchronization is an important step towards meeting the power and phase noise requirements of commercial applications, our demonstration of robust synchronization over very large distances, and for a large number of nanoconstrictions, also opens up additional intriguing possibilities in magnon spintronics⁵⁰ and spin wave computing^{51–54}. Whereas all nanoconstrictions in this work were placed on a single line, we expect more complex nanoconstriction arrangements to also operate successfully and show synchronization. One may, for example, envisage spin wave

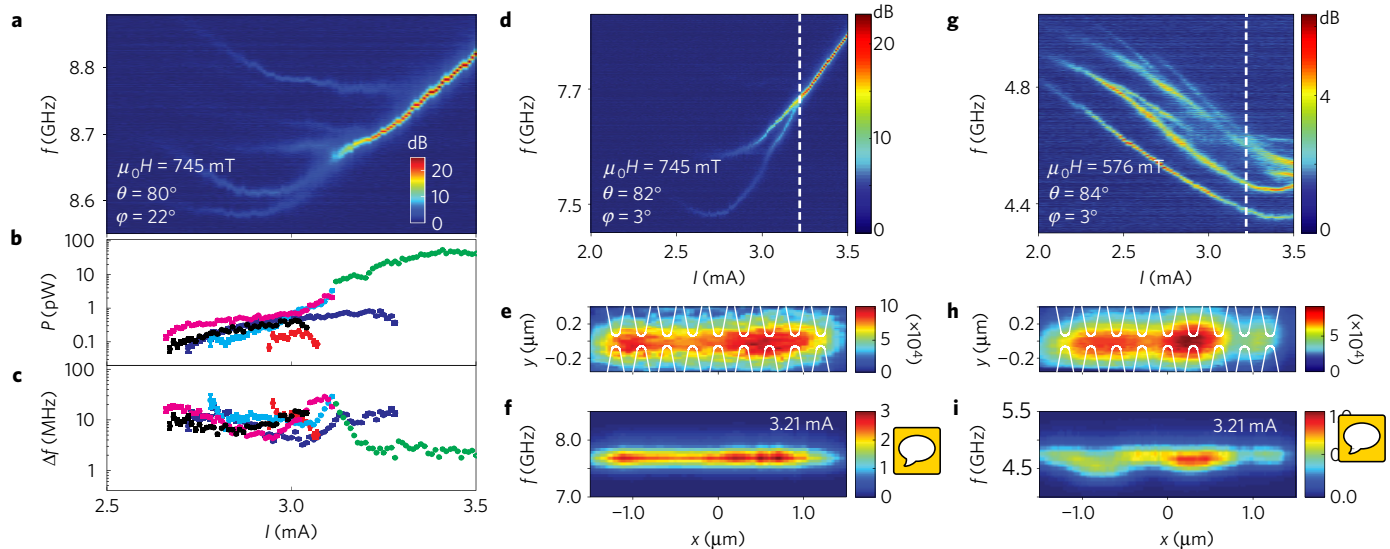


Figure 6 | Multiple SHNO synchronization. **a**, Power spectral density versus current of the SHNO in Fig. 1, with nine nanoconstrictions with $w = 120$ nm width each, separated by $d_{cc} = 300$ nm from each other, in an applied field of 745 mT along $\varphi = 22^\circ$, and $\theta = 80^\circ$. **b**, Total power of the extracted individual peaks and the globally synchronized peak. **c**, Linewidth of the extracted peaks. **d**, Power spectral density versus current of the SHNO in an applied field of 745 mT along $\varphi = 3^\circ$ and $\theta = 82^\circ$. **e**, μ -BLS spatial map taken at synchronization $I_{\text{dr,e}} = 3.21$ mA. **f**, μ -BLS frequency map of the central horizontal line passing through all nanoconstrictions, at $y = 0$. **g**, Power spectral density versus current of the SHNO in an applied field of 576 mT along $\varphi = 3^\circ$ and $\theta = 84^\circ$. **h**, μ -BLS spatial map taken at $I_{\text{dr,e}} = 3.21$ mA. **i**, μ -BLS frequency map of the central horizontal line passing through all nanoconstrictions, at $y = 0$.

majority gates^{52,54} where three or more smaller nanoconstrictions are connected to a larger nanoconstriction such that they all operate at the same current density and approximately the same frequency. When driven into mutual synchronization, the phase of the output nanoconstriction will then acquire the majority phase value of the inputs. Wave computing can also be used in oscillatory neural networks, and as neural synchronization has been demonstrated to govern associative memory processes⁵⁵, SHNO networks with tunable coupling strengths may mimic neurons in the brain⁵⁶.

The relative ease of fabrication of strongly synchronized nanoconstriction SHNOs will hence enable the design and fabrication of more complex and highly networked nanoconstriction-based architectures where both digital and analog spin-wave-based computing can be realized.

Methods

Methods, including statements of data availability and any associated accession codes and references, are available in the online version of this paper.

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Author contributions

A.A.A. designed the devices. P.D. and A.H. fabricated the devices. A.A.A., P.D. and A.H. performed all electrical measurements. R.K.D. and A.A.A. built the μ -BLS microscope. A.A.A. carried out all optical measurements. A.A.A. and M.D. performed the micromagnetic simulations. All authors contributed to the data analysis and co-wrote the manuscript.

Additional information

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Correspondence and requests for materials should be addressed to J.A.

Competing financial interests

The authors declare no competing financial interests.

Methods

Sample fabrication. A bilayer of 6 nm Pt and 5 nm Py ($\text{Ni}_{80}\text{Fe}_{20}$) was magnetron sputtered in a system with a base pressure lower than 3×10^{-8} torr at room temperature onto a 20 mm \times 20 mm piece of sapphire C-plane substrate, and then *in situ* covered with 5 nm SiO_2 to prevent the permalloy layer from oxidation. The bilayer was then patterned into $4 \mu\text{m} \times 12 \mu\text{m}$ rectangles with different bow-tie-shaped constrictions by e-beam lithography and subsequent argon ion milling using negative e-beam resist as the etching mask. The devices were then covered with an additional 50 nm SiO_2 layer to protect them from oxidation during measurements. A coplanar waveguide provides electrical contacts and is defined by optical lithography, reactive ion etching of the protective SiO_2 layer, sputtering of copper, and lift-off.

Electrical characterization. All measurements were performed at room temperature. We mounted the sample with a fixed in-plane angle on a rotatable sample holder between the poles of an electromagnet. The current bias was applied through a high-frequency bias-T and the resulting radiofrequency oscillations amplified by a low-noise amplifier and recorded with a high-frequency spectrum analyser using a low-resolution bandwidth of 300 kHz. Figure 2 shows single scan data to minimize the time the device spends at high current. All other electrical microwave measurements (Fig. 6 and Supplementary Methods) are from four averaged scans at each current, which reduces the scatter substantially. The obtained spectra were corrected to correspond to the power emitted by the device, taking into account the amplifier gain, the losses from the radiofrequency components and cables, and the impedance mismatch between the device and the 50 Ω measurement line. The spectra were fitted with a single symmetric Lorentzian to extract the auto-oscillation frequency, power and linewidth.

μ -BLS characterization. The magneto-optical measurements were performed using room-temperature micro-focused BLS measurements. Spatially resolved maps of the magnetization dynamics are obtained by focusing a polarized monochromatic 532 nm single-frequency laser (solid state diode-pumped) using a high numerical aperture ($\text{NA} = 0.75$) dark-field objective, which yields a diffraction limited resolution of 360 nm. The scattered light from the sample surface is then analysed by a high-contrast six-pass Tandem Fabry–Perot interferometer TFP-1 (JRS Scientific Instruments). The obtained BLS intensity is proportional to the square of the amplitude of the magnetization dynamics at the corresponding frequency. The μ -BLS set-up is equipped with a spectrum analyser

connected to the sample via bias-T to measure the electrical and the optical signals simultaneously.

Micromagnetic simulations. The micromagnetic simulations were done using the graphics processor unit (GPU)-based finite-difference micromagnetic solver MuMax3 (ref. 57). The SHNO is modelled by $1,024 \times 1,024 \times 1$ cells with a cell size of $3.9063 \times 3.9063 \times 5 \text{ nm}^3$. The parameters used in the simulation include the saturation magnetization $\mu_0 M_s = 0.754 \text{ T}$, exchange stiffness $A_{\text{ex}} = 10 \times 10^{-12} \text{ J m}^{-1}$, and the damping constant $\alpha = 0.022$, all determined from experiments on blanket films. In addition to the applied field $H = 0.72 \text{ T}$, the charge current distribution and the resulting Oersted field landscape is calculated using COMSOL Multiphysics simulation software (www.comsol.com). The corresponding spin current is then calculated from the simulated charge current in the Pt layer (see, for example, Fig. 1c) and converted into a SHE-generated spin current in the $-\hat{z}$ -direction assuming a spin Hall angle, $J_s/J_c = \theta_{\text{SH}} = 0.08$. The spin Hall angle is also determined experimentally from the same bilayer using spin-torque-induced ferromagnetic resonance (ST-FMR) on a 1- μm -wide stripe, a measurement similar to that performed in ref. 58 and found to be $\theta_{\text{SH}} = 0.08 \pm 0.01$ in our bilayer system. The spin current is approximated to have a 100% spin polarization along the $-\hat{x}$ -direction. The auto-oscillation frequency is obtained by performing the FFT of the simulated time evolution (250 ns total) of the averaged magnetization after an initial 60 ns of transient behaviour is disregarded. By performing a discrete Fourier transform of each simulation cell, a full spatial map of the generated auto-oscillations is extracted. The free-running oscillators are modelled one by one in the full-scale pair geometry by suppressing the spin current density on either smaller or larger nanoconstriction sites. This allows for a direct comparison with the response of the simultaneously acting (interacting) oscillators.

Data availability. The data that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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